



Differential privacy and noisy confidentiality concepts for European population statistics

2021 Joint UNECE/Eurostat Expert Meeting on SDC, 1 – 3 December 2021
Tabular data session

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Unit F2 – Population and migration

Outline

1. Intro: evolution of SDC (in population tables)
2. Noisy concepts: bottom-up and top-down
3. Risks: exploiting and massive averaging
4. Utility: (noise) tail wagging the (statistic) dog
5. Outro: the 2021 EU census picture

Intro: evolution of SDC (in population tables)

20th century lore:

- must protect **individuals**
- therefore treat **small counts...**
- ... and ensure **consistency...**
- ... and ensure **consistency...**
- ... and ensure **consistency...**

| SEX \ POB* | Total | Country | Outside |
|------------|-------|---------|---------|
| Total | 42 | 35 | 7 |
| Male | 22 | C | C |
| Female | 20 | C | C |

* Place of birth (POB)

→ looks easy, but is generally **neither simple nor efficient**

Intro: evolution of SDC (in population tables)

21th century state of the art:

- database reconstruction theorem ([Dinur and Nissim, 2003](#))

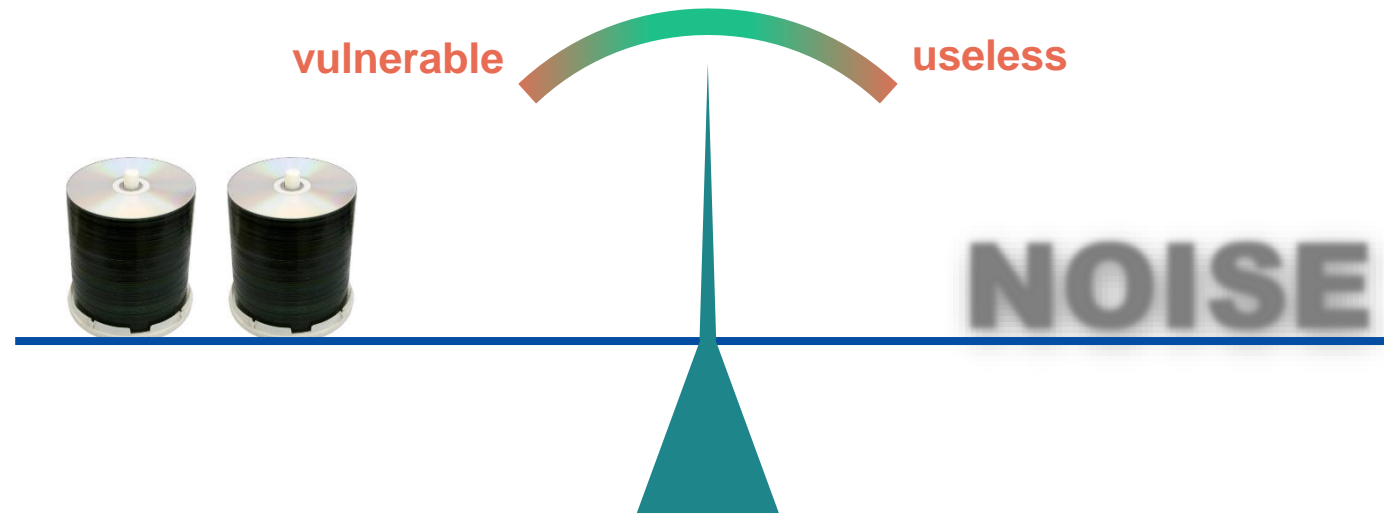
Too many statistics, published too accurately, allow full & accurate reconstruction of all the input microdata...

(example e.g. in [U.S. Census Bureau, 2018a, 2018b](#))

Intro: evolution of SDC (in population tables)

21th century state of the art:

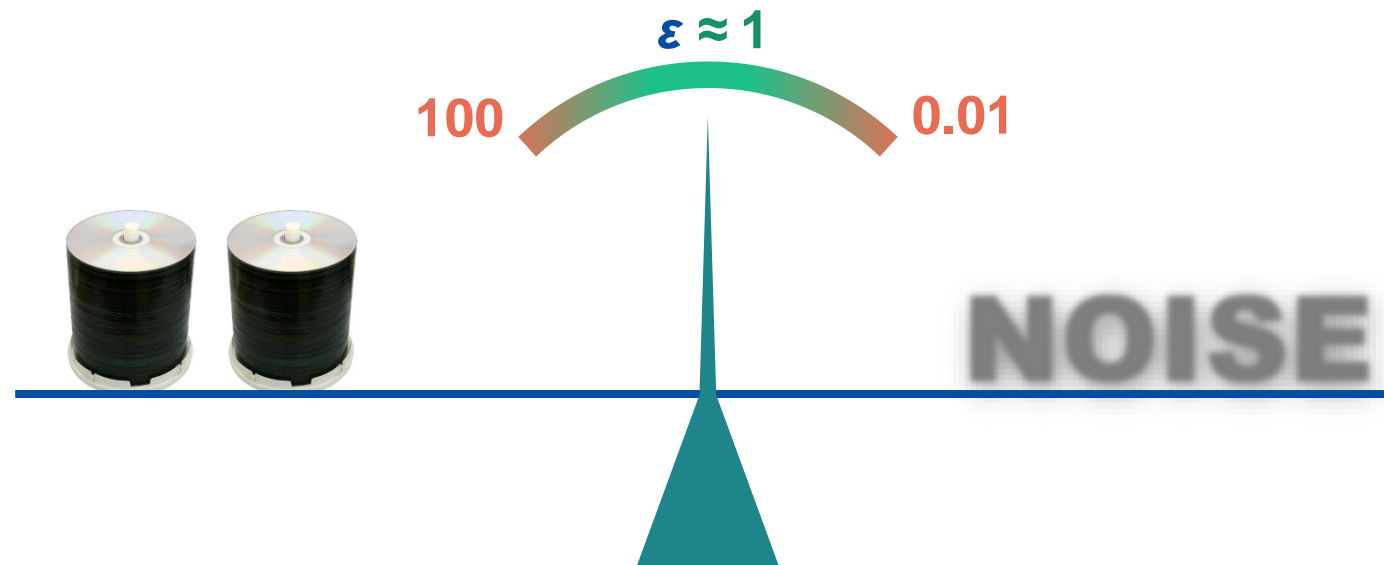
- database reconstruction theorem ([Dinur and Nissim, 2003](#))



Noisy concepts: top-down

Differential privacy (DP) picture:

- introducing global privacy budget ϵ ([Dwork et al., 2006](#))



Noisy concepts: top-down or *risk-driven*

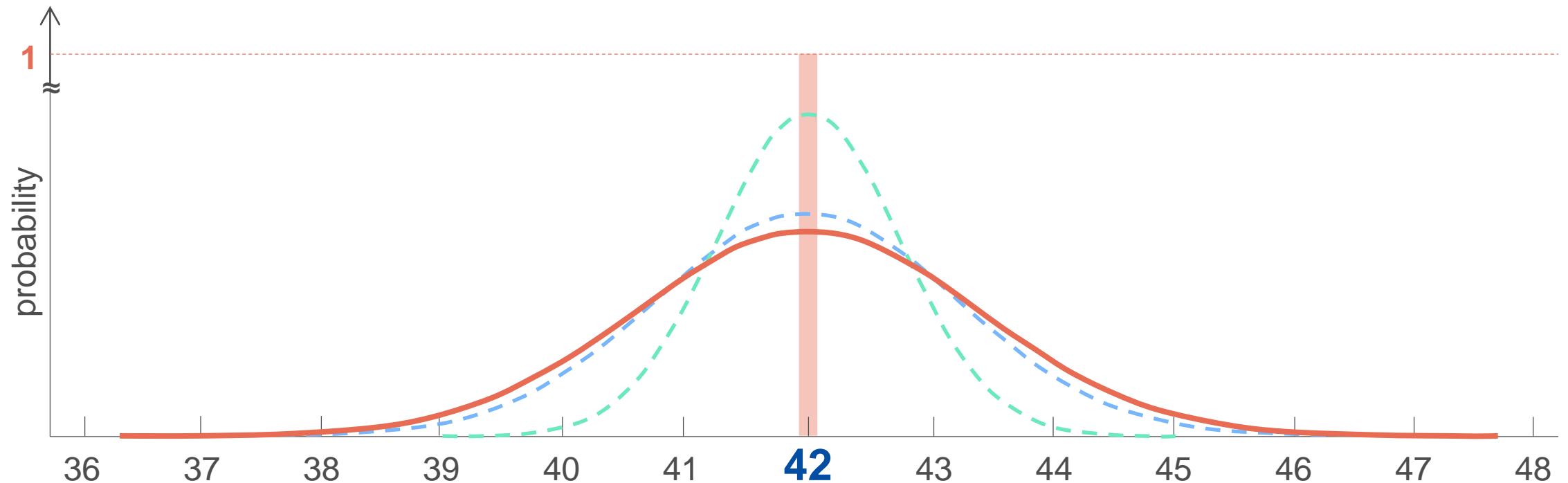
Differential privacy (DP) picture:

- introducing global privacy budget ϵ ([Dwork et al., 2006](#))
- promise: strong **global privacy guarantee** ... but **local noise size**?



Noisy concepts: bottom-up

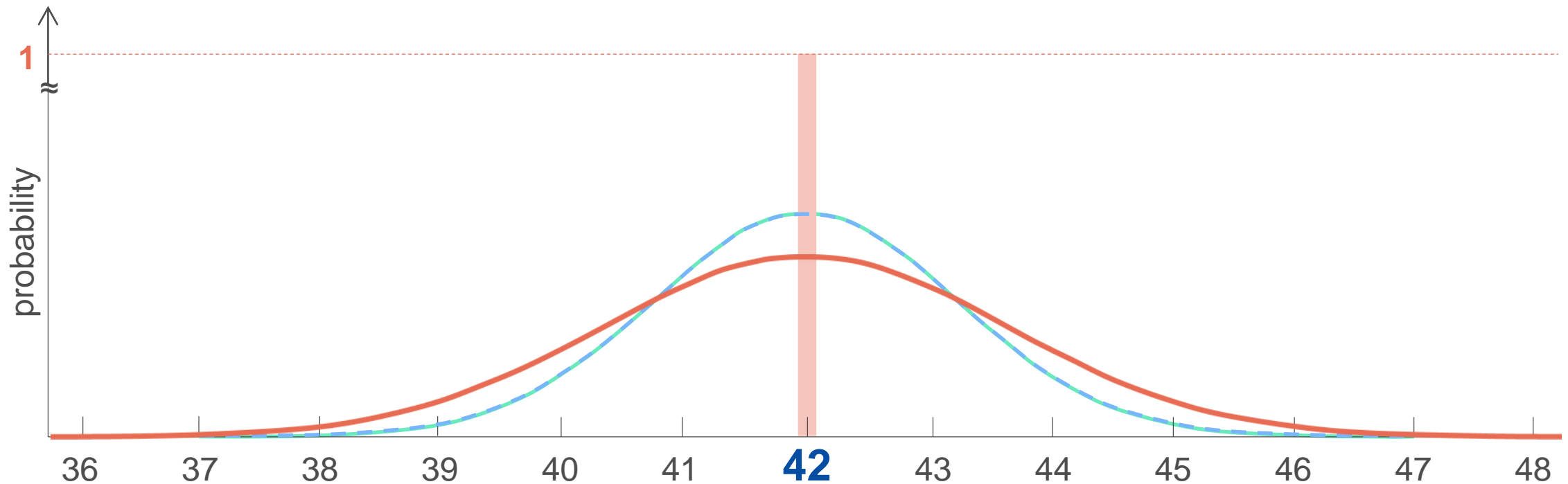
... a closer look at **single statistic** level – e.g. total population in the area:



intrinsic uncertainty: ± 2
protective noise added: ± 1
total uncertainty: ± 2.2

Noisy concepts: bottom-up

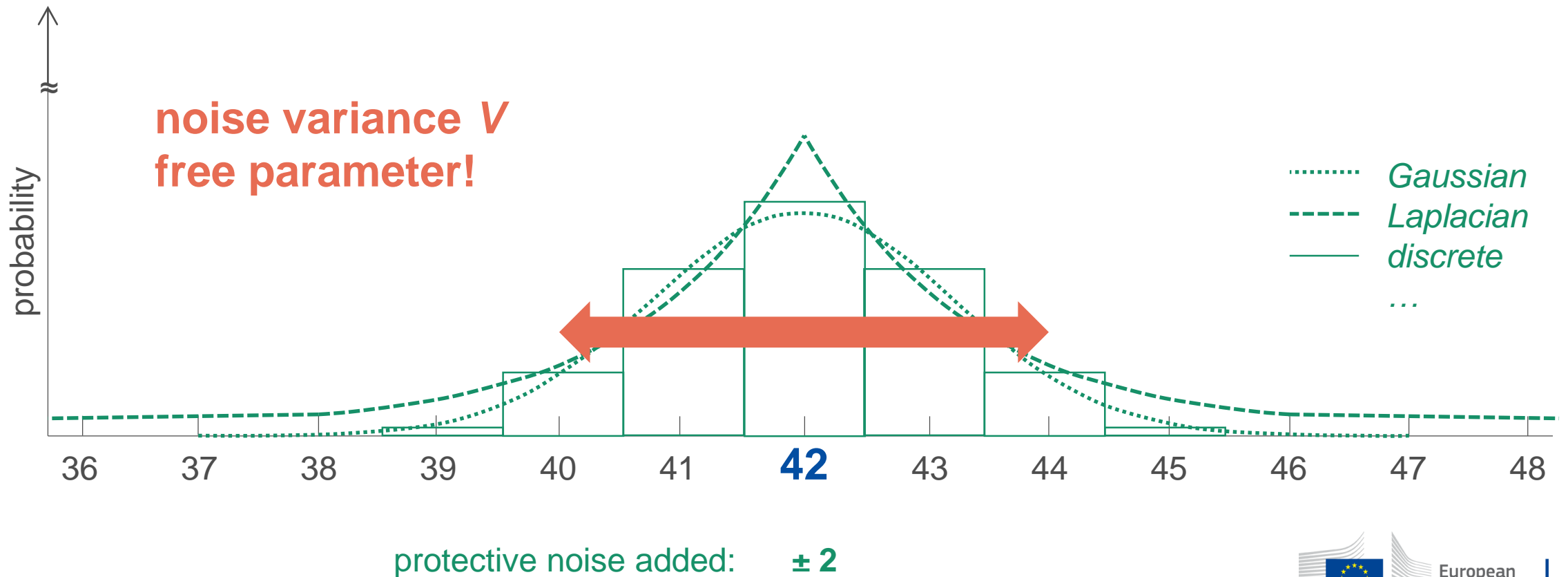
... a closer look at **single statistic** level – e.g. total population in the area:



intrinsic uncertainty: ± 2
protective noise added: ± 2
total uncertainty: ± 2.8

Noisy concepts: bottom-up or *utility-driven*

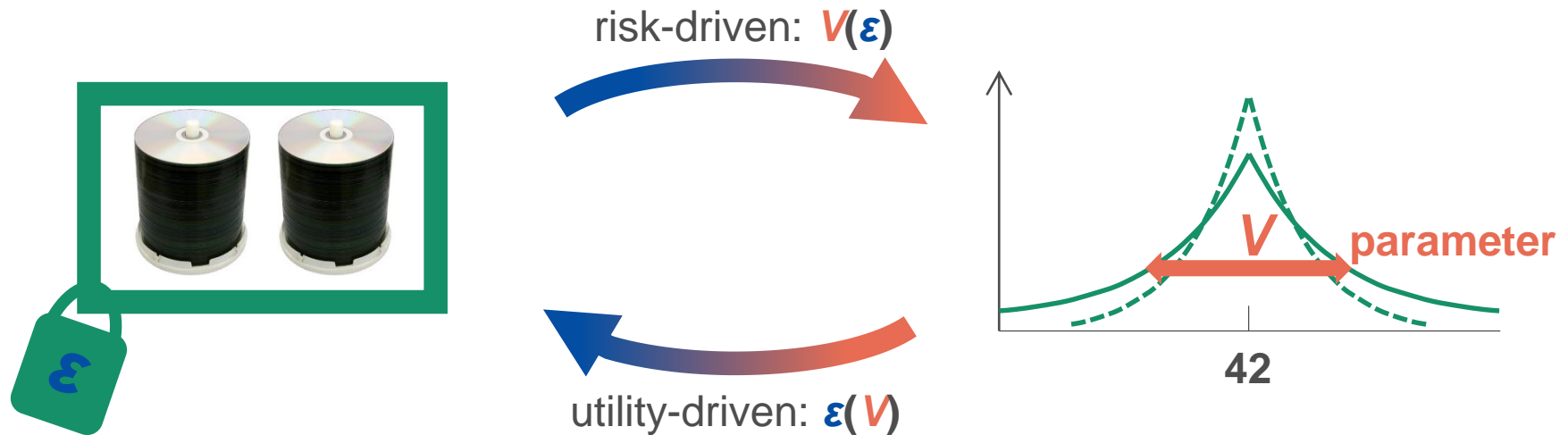
... a closer look at **single statistic** level – e.g. total population in the area:



Noisy concepts: bottom-up or *utility-driven*

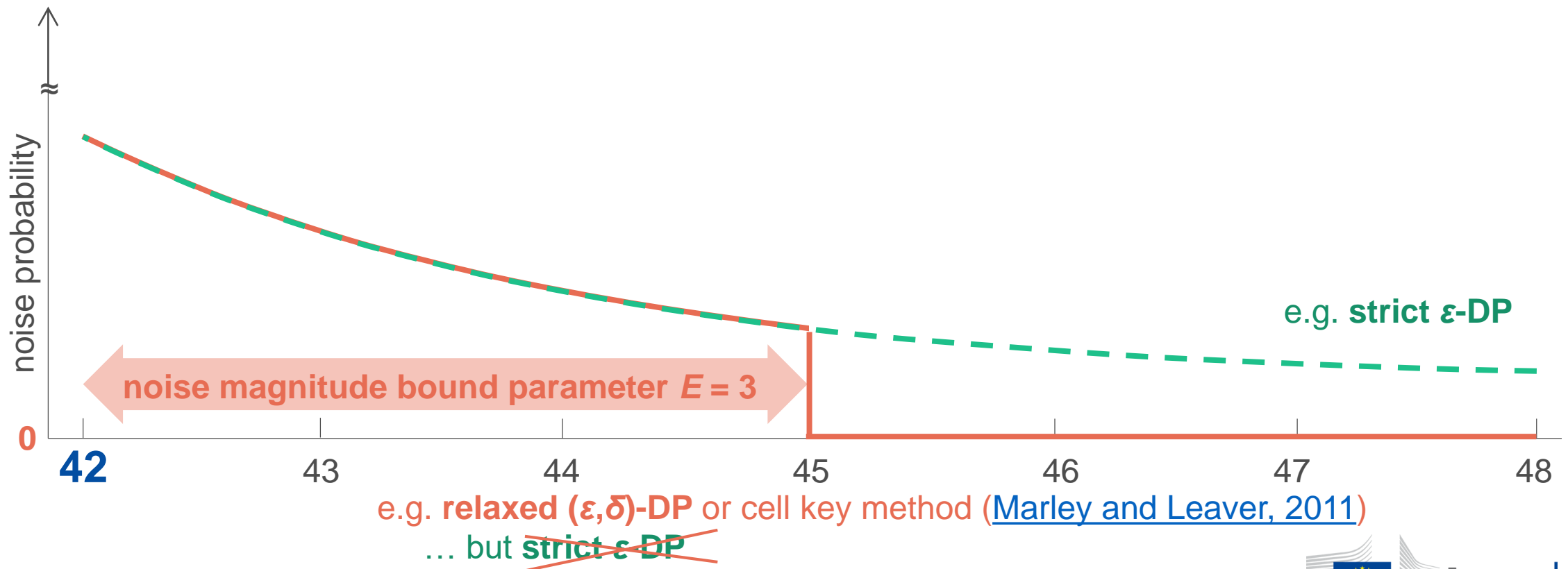
Utility driven picture:

- parametrising local noise impact at single statistic level
- promise: strong **utility guarantees** ... but **global privacy level?**



Noisy concepts: bottom-up or *utility-driven*

- Noise distributions – part 2: how long is the **tail**?



Risks: exploiting table constraints

- Now would you bet all your money on a guess for the **true count** of the ...

- ... total population?
- ... **country-born males (= 17)**
- ... total females?
- ... total foreign-born?

| SEX \ POB | Total | Country | Outside |
|-----------|-------|-----------|---------|
| Total | 42 | 37 = 35+2 | 7 |
| Male | 23 | 15 = 17-2 | 4 |
| Female | 21 | 16 = 18-2 | 3 |

each count with noise variance $V = 1$
and noise bound $E = 2$

- How often does this happen?

$$\# \text{ of constraint } n\text{-tuples in output} \times \Pr(\text{noise} = \pm E)^n$$

fixed by output tables

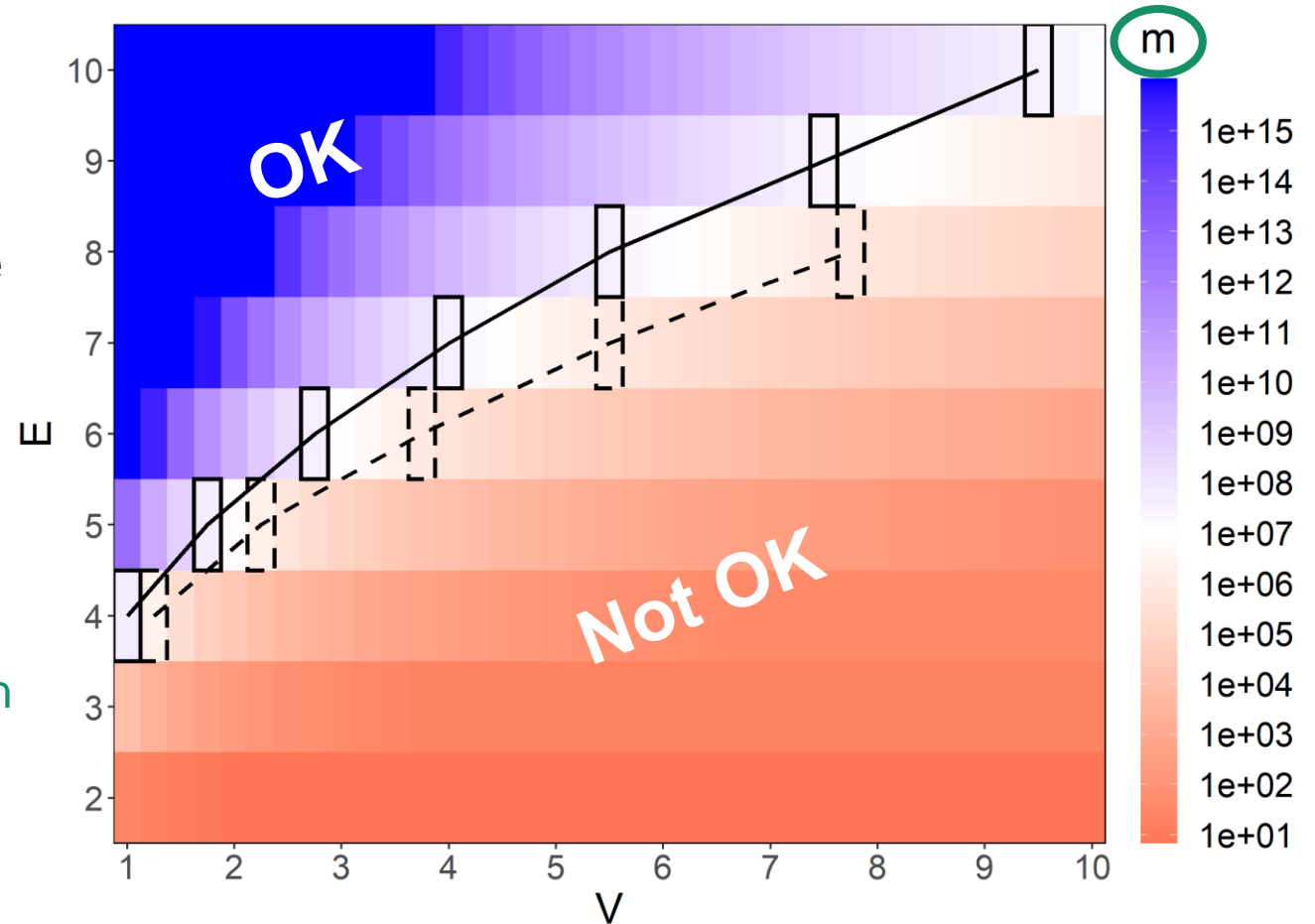
fixed by noise parameters V and E

Risks: exploiting table constraints

→ Knowing the full output, the risk can be quantified systematically – e.g. for the 2021 EU census output:

m : number of 3-tuples needed in output to get ca. one E -disclosive noise pattern

black boxes showing where m exceeds the number of available 3-tuples for Malta (dashed) and Germany (solid)



Risks: massive averaging

- How many independent observations t of “total population” are in this table?

$t = 1$

$t = 2$

$t = 3$

$t = 4$

| SEX \ POB | Total | Country | Outside |
|-----------|-------|---------|---------|
| Total | 42 | 37 | 7 |
| Male | 23 | 15 | 4 |
| Female | 21 | 16 | 3 |

each count with noise variance $V = 1$

- average variance:

$$\bar{V} = \frac{k}{t^2} V = \frac{9}{4^2} 1 = 0.5$$

fixed by output tables

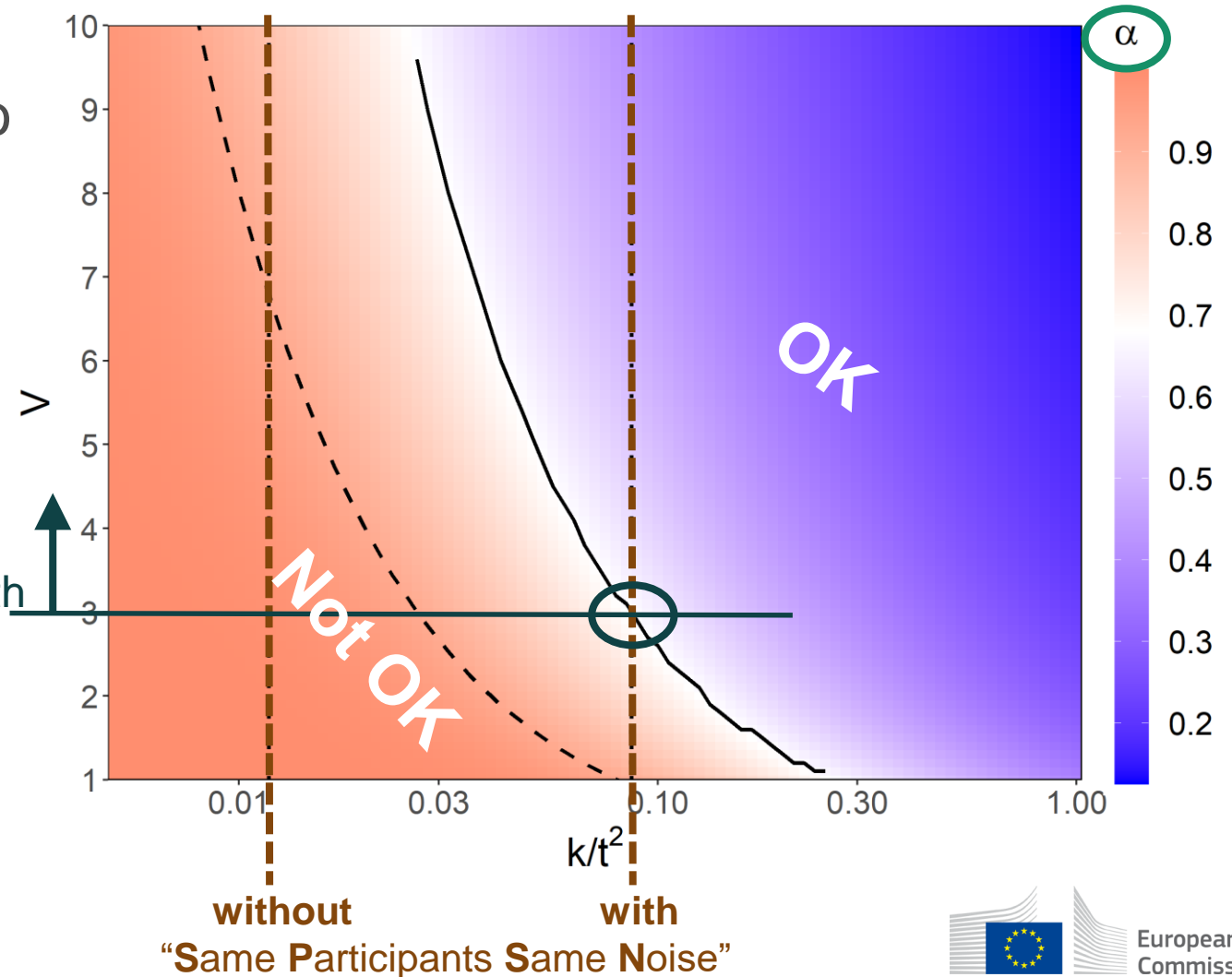
noise parameter

Risks: massive averaging

→ Knowing the full output, also this risk can be quantified systematically – e.g. for the 2021 EU census output:

intersection of $\alpha = 68\%$ contour with smallest k/t^2 value (with SPSN)

α : c.l. of obtaining correct rounded integer count after averaging

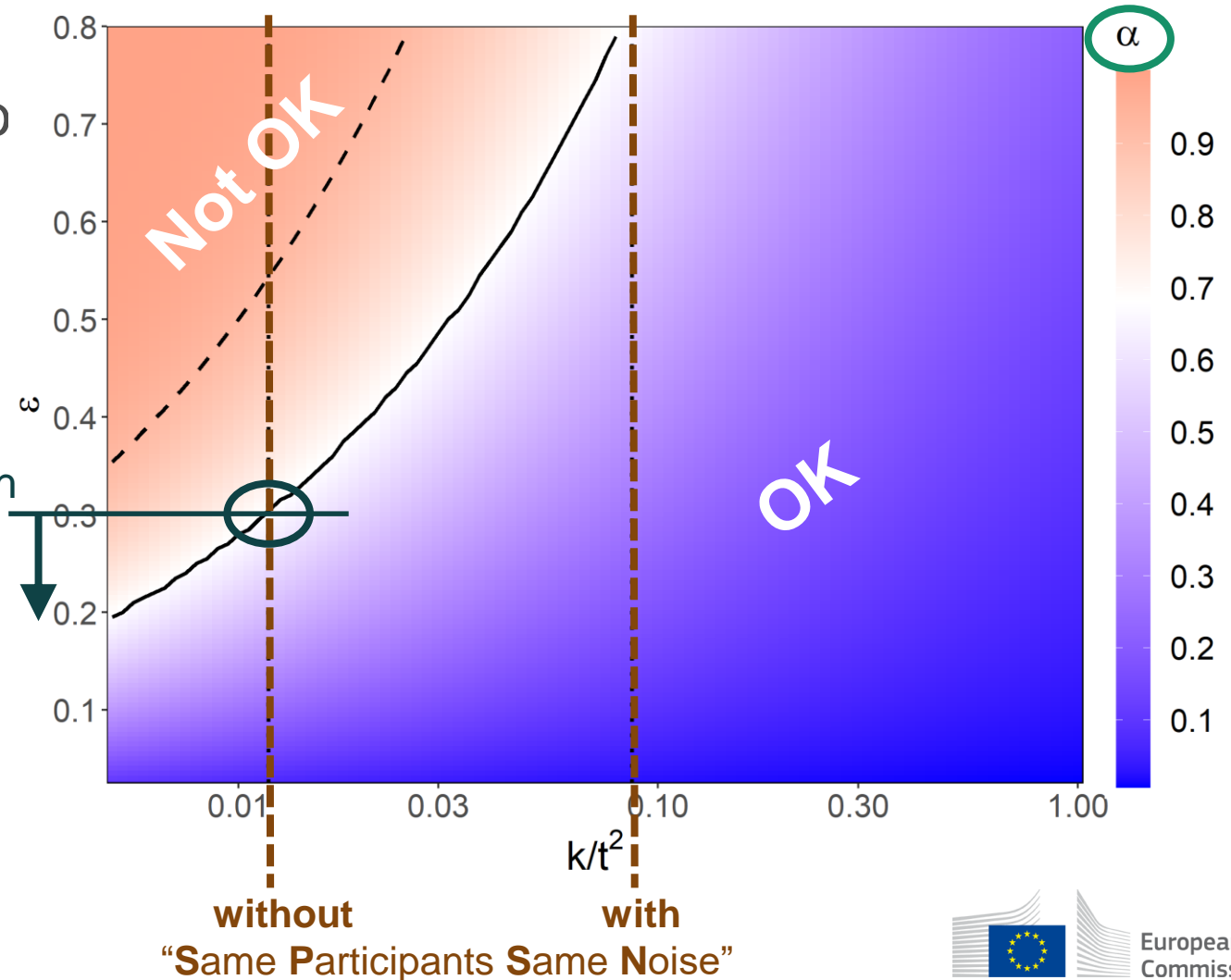


Risks: massive averaging – *DP picture*

→ Knowing the full output, also this risk can be quantified systematically – e.g. for the 2021 EU census output:

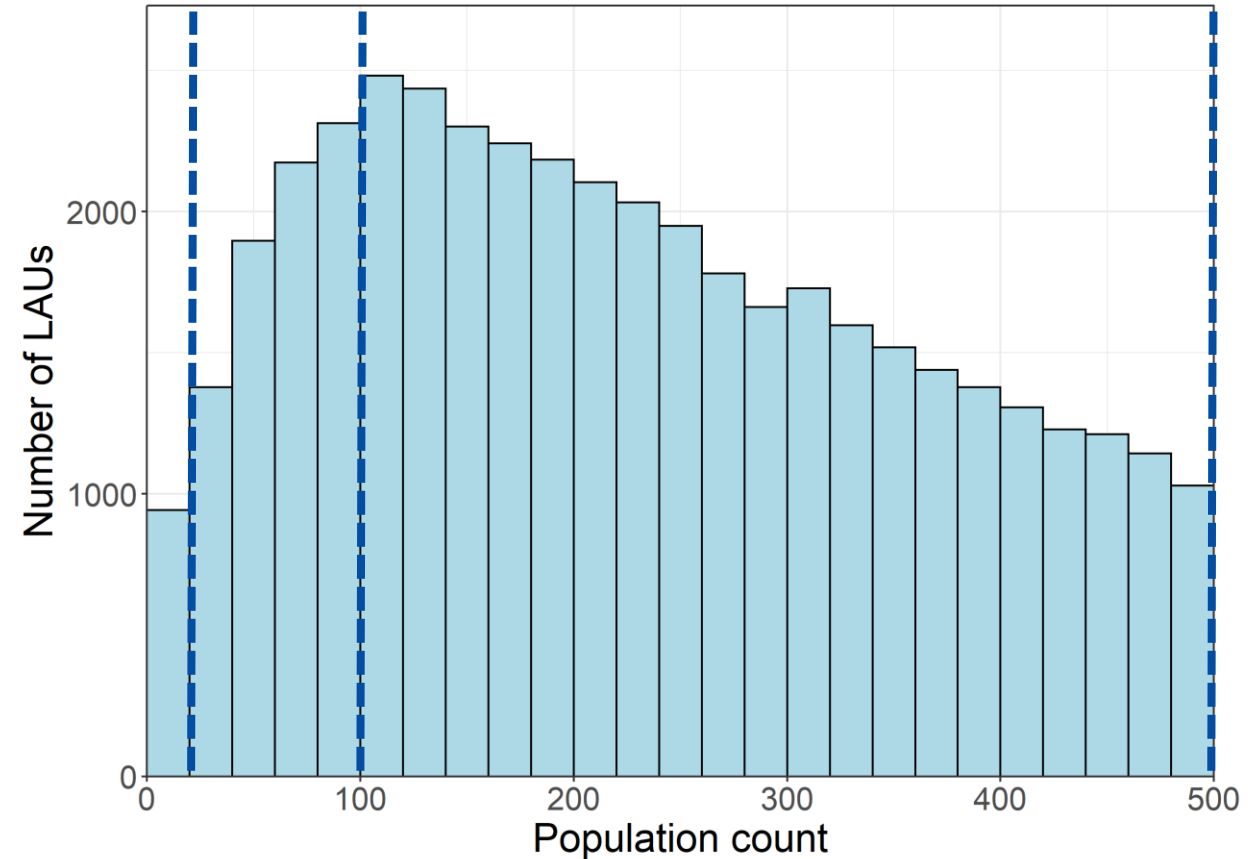
intersection of $\alpha = 68\%$ contour with smallest k/t^2 value (without SPSN)

α : c.i. of obtaining correct rounded integer count after averaging



Utility: (noise) tail wagging the (statistic) dog

- 2021 EU census: ca. 110 000 **L**ocal **A**dministrative **U**nits (~ municipalities), of which
 - 43 395 with <500 people
 - 8 502 with <100 people
 - 866 with <20 people
- Could we accept here e.g. $\Pr(|\text{noise}| > 100) = 0.1\%$ or more?
 - Yes
 - No

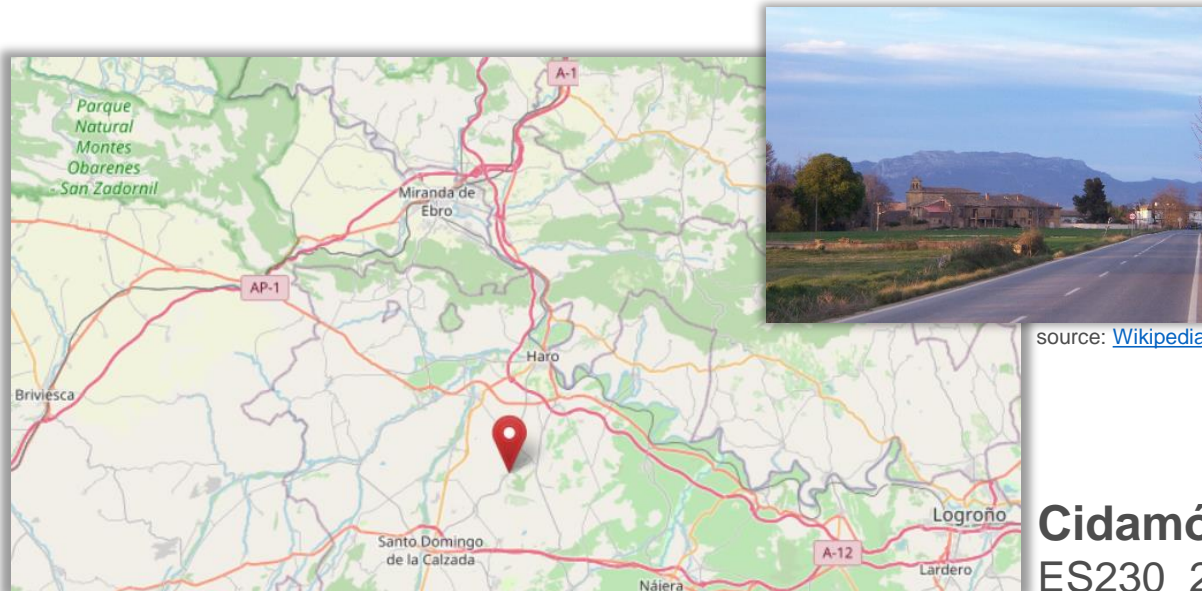


Utility: (noise) tail wagging the (statistic) dog

- mainly a problem of **unbounded noise**

Recall: Noise magnitude bound parameter ϵ , “cutting off” the tail, is **forbidden** in strict ϵ -DP

- E.g. 2020 test setup of [U.S. Census Bureau \(2019\)](#) with moderate tabular $\epsilon = 0.1$



source: [Wikipedia](#)

Cidamón, La Rioja, Spain
ES230_26048

| | 2011 census | strict ϵ -DP |
|--------|-------------|-----------------------|
| Total | 30 | -17 |
| Male | 20 | -1 |
| Female | 15 | -9 |

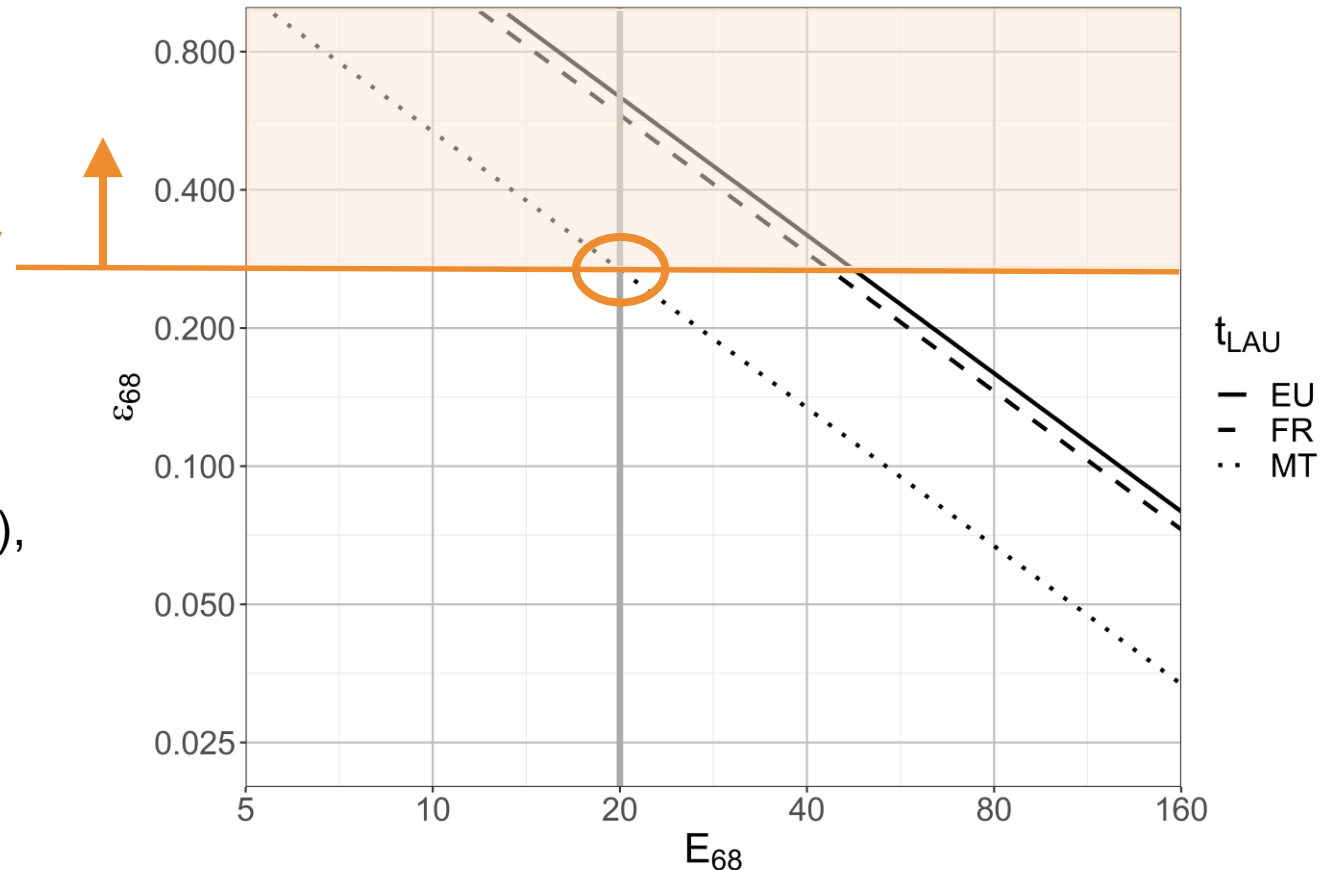
source: [OpenStreetMap](#)

Utility: (noise) tail wagging the (statistic) dog

- mainly a problem of **unbounded noise**

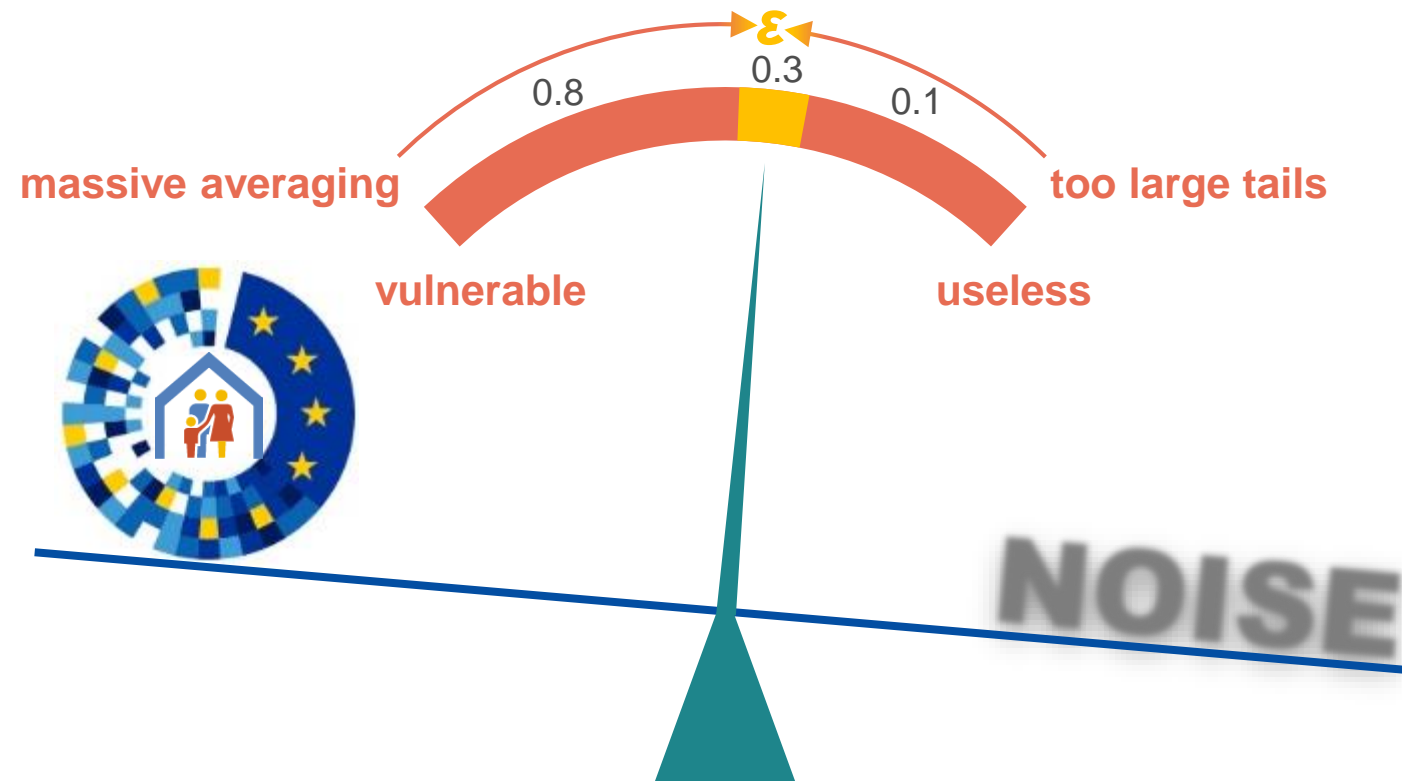
intersection of $\alpha = 68\%$ contour for Malta with $E = 20$

$\alpha = 68\%$ contours of getting ca. one LAU count noise $> E$ for Malta (dotted), France (dashed), whole EU (solid)



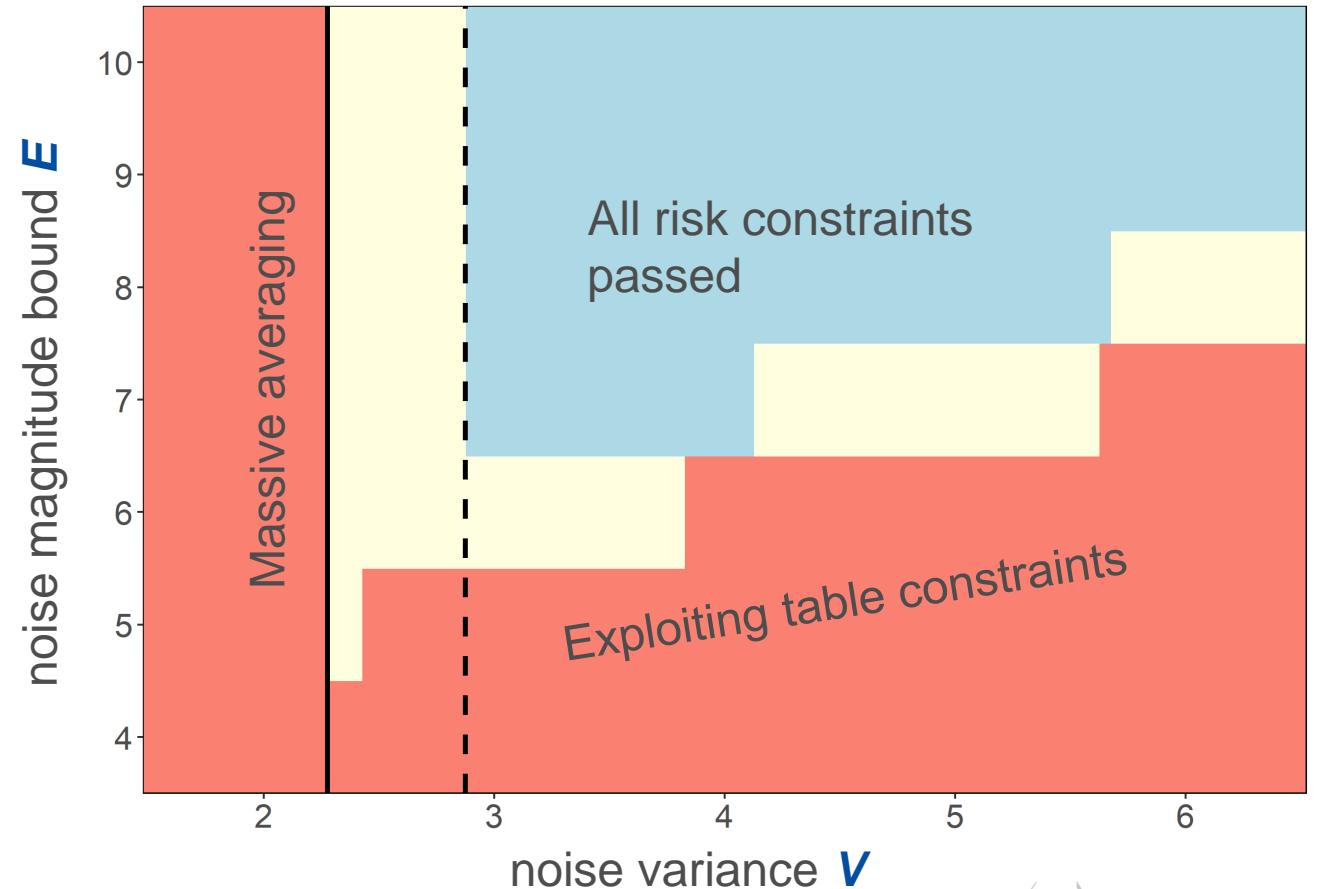
Outro: the 2021 EU census picture

- risk + utility constraints on **tabular ϵ** for whole 2021 EU census output



Outro: the 2021 EU census picture

- whole 2021 EU census output
- risk constraints on bottom-up parameter space $V - E$
- utility controlled directly by V and E (utility-driven)
- e.g. cell key method recommended for 2021 EU census ([ESSnet, 2017, 2019](#))



Thank you



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Slides 5-7 and 11: CD stack icon, source: photo by [lilieks](#) from [Freelimages](#); Slide 20: map section, source: screenshot from [OpenStreetMap](#); Slide 19: view of Cidamón, source: photo by [Bigsus](#) from [Wikipedia](#); Slide 19: EU census icon, source: [Eurostat](#); Slide 21: European Statistical System logo, source: [Eurostat](#)



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