

The development of Variable Plot Sampling

by Kim Iles

Timber Measurements Society

Imperial measurements

There are only 3 serious methods for timber cruising.

- **Fixed Plots** (ancient, but simple)
- **Variable Plots** (1946, end of WWII)
- **3P Sampling** (1960's, the beetles)

What is the trend?

- Each newer method further divides the field work into parts that are :

- Quick vs. slower



- Unskilled vs. skilled work



- Estimates, with a correction



Efficiency issue

Accuracy issue

Walter Bitterlich had an idea, based on circular tree cross-sections.

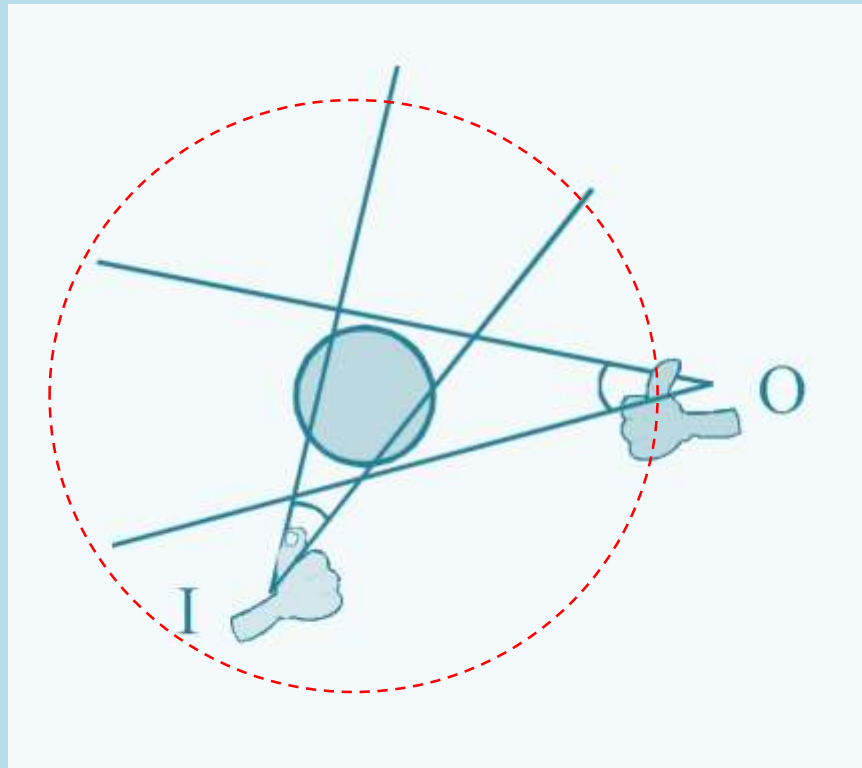


Bitterlich – 1946, said ...

- Just “count” trees – that gives you **basal area**.
- Counting is in percent (no units involved).
- You then assign units (**43,560 ft² /acre**)
(10,000 m² /ha)
- The angle gives the “Basal Area Factor”

Are you “in” or “out” of an invisible circle around each tree?

- Just use an angle to decide that.
- Imagine using your thumb.



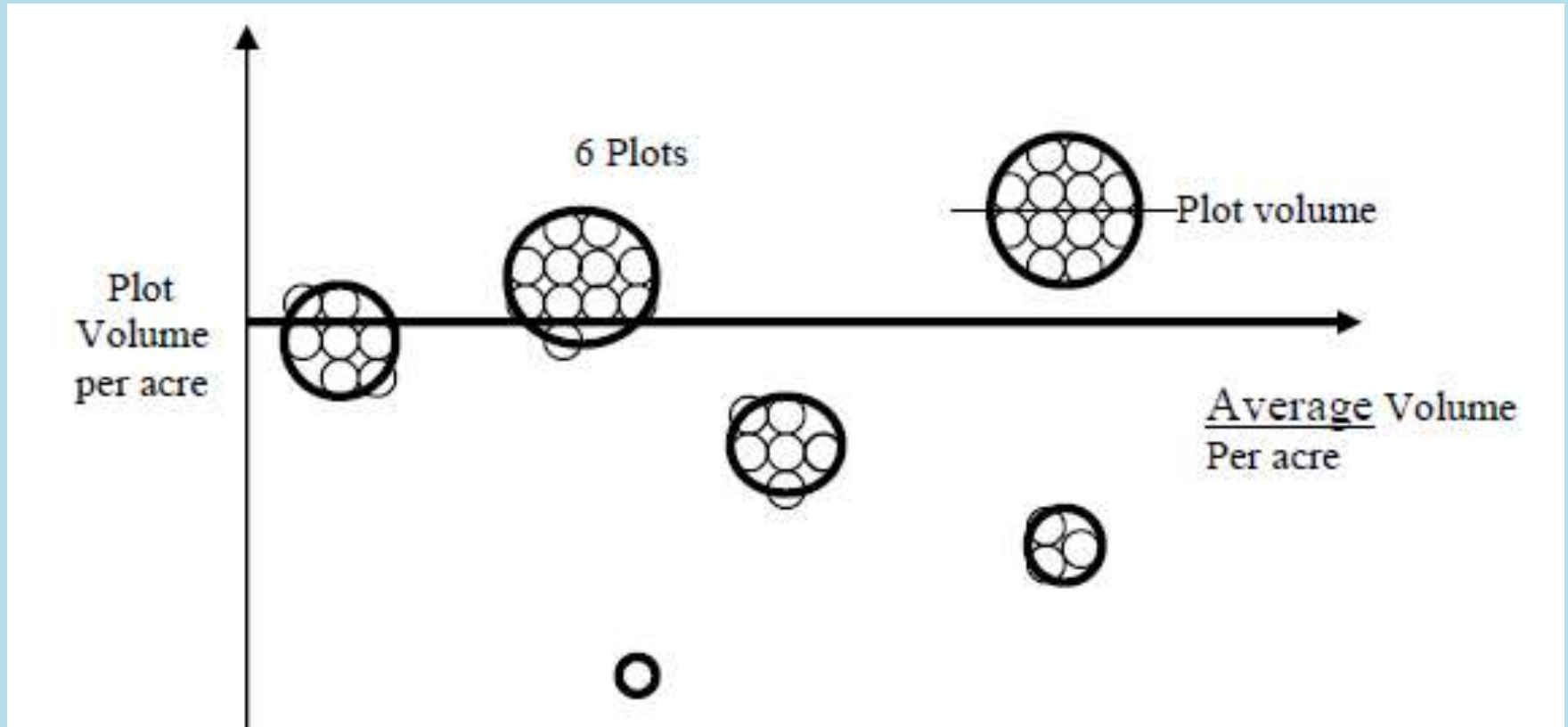
**Lew Grosenbaugh immediately
reads about this idea in 1947.**



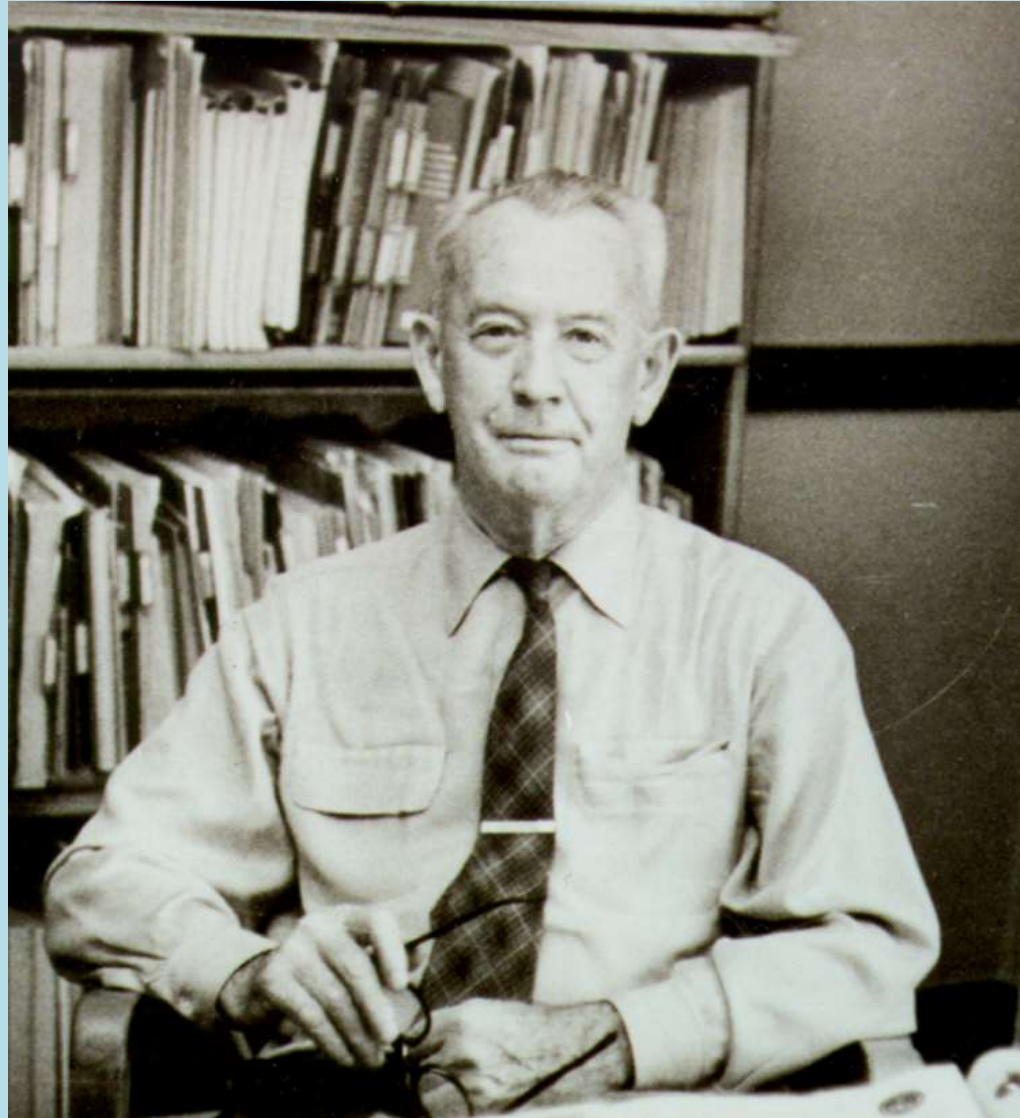
He thinks ...

- If you have the basal area, just find out how much is “sitting on each square foot” to calculate **any** other stuff.
- This **Value / Basal Area Ratio** is called “**VBAR**”.

Grosenbaugh treated it like a Fixed Plot



Next, Don Bruce



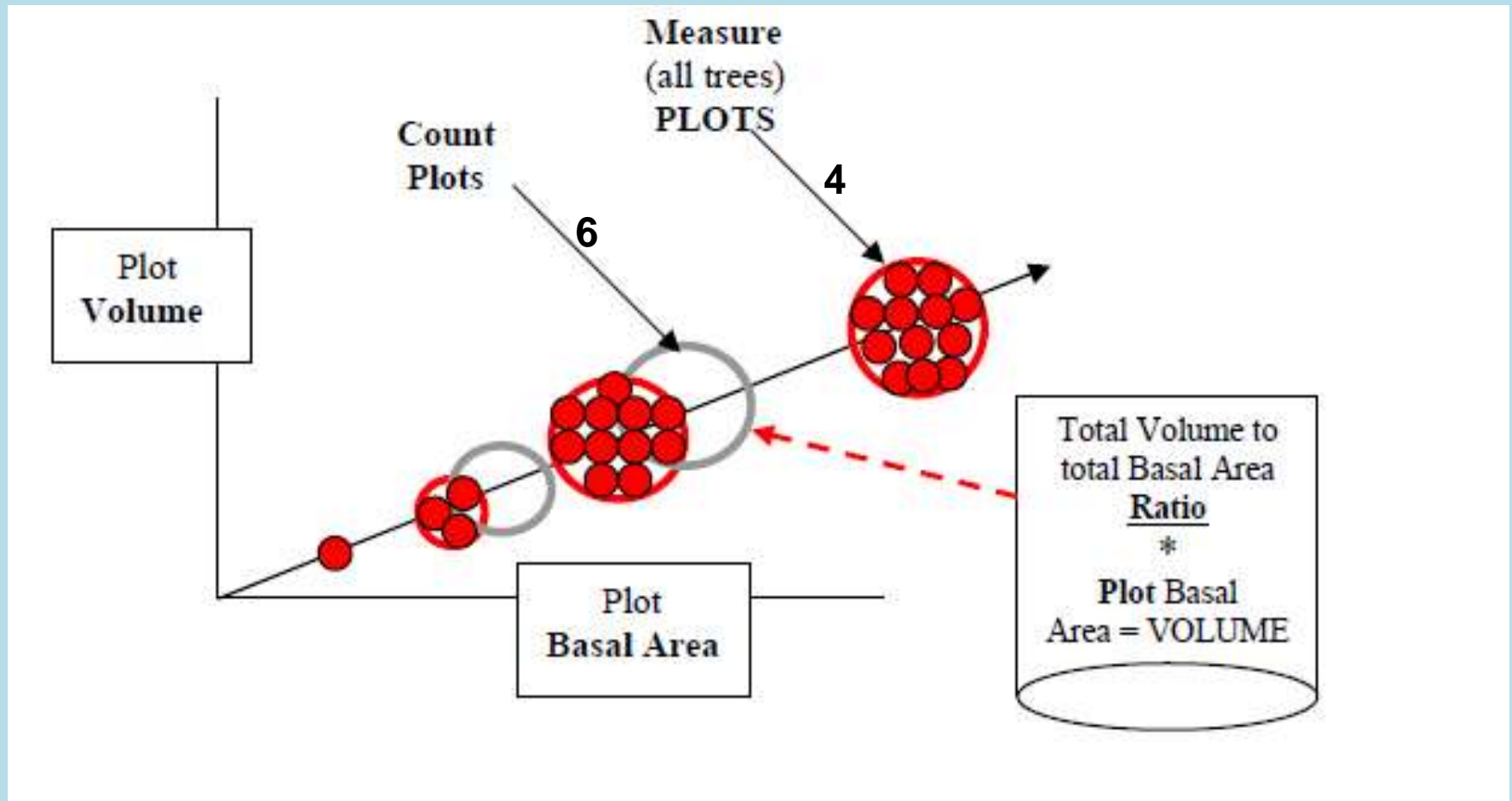
Mason Bruce and Girard (1950) introduce “Count and Measure” plots.

- Just measure the trees on some of the plots, only counting trees on the others.
- Sum **plot** Vol's / Sum **plot** BA's = **VBAR Ratio**
- If plots were too far apart, people lost their nerve ... at about a 4 or 5 counts per measure.

How it is done

- 1) Do all plots for some easy and quick variable (basal area, in this case).
- 2) Measure some plots for a ratio, then use the ratio to convert all the other basal areas.
- 3) PS ... You do the same tree measurements with any of these systems.

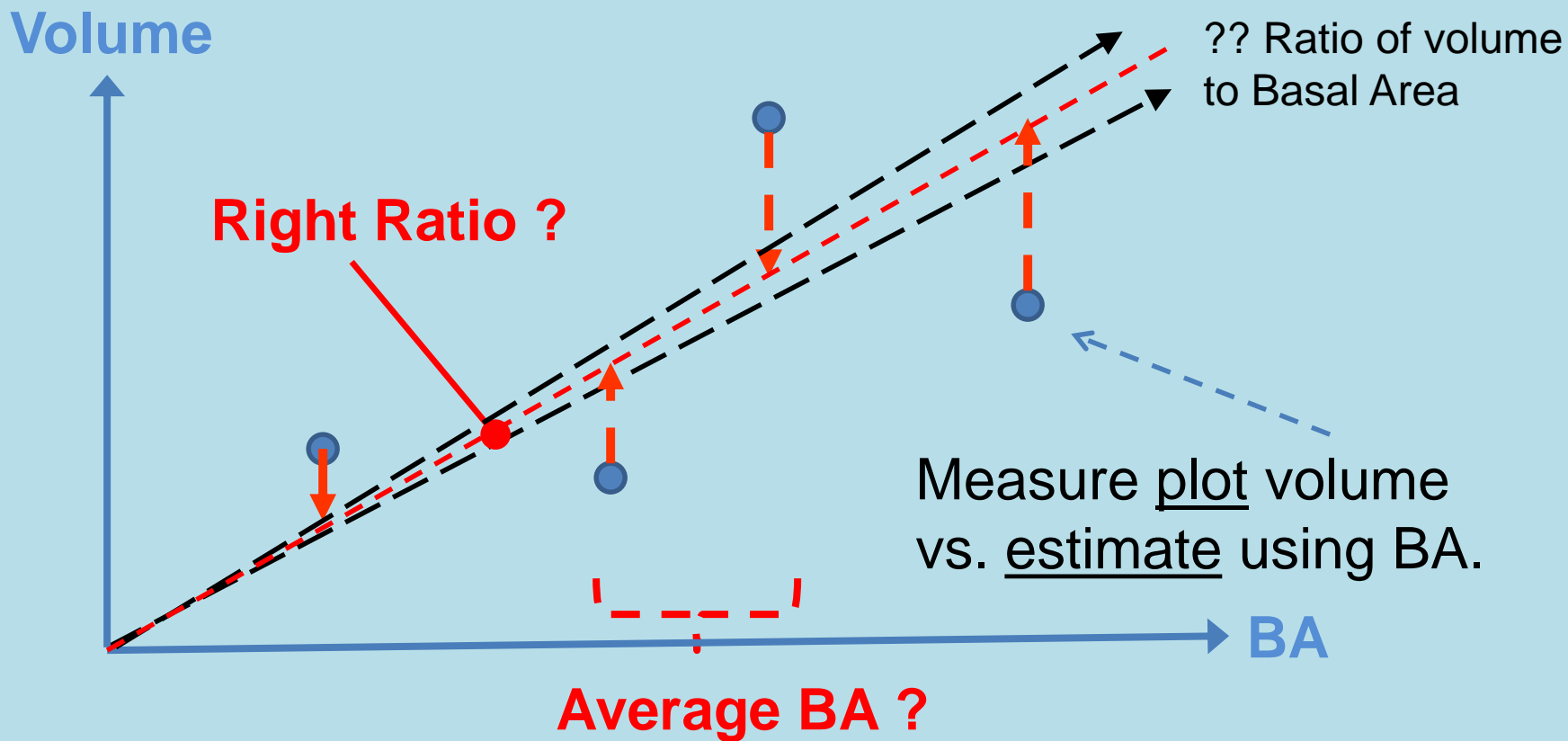
It's called "Double Sampling"
and uses Plot volumes & BA's



Key points

- 1) These trees are measured in “clusters” on the measured points.
- 2) Many counts are done to improve the final result.

There is sampling error in the average Basal Area and the Vol/BA correction.



The statistical formula is messy
for Double Sampling

Known as

“Johnson’s Formula” in forestry

Next, DAVE Bruce – the son



He said : A “Product Estimator”
could also be used here.

(Dave also invented the wedge prism)

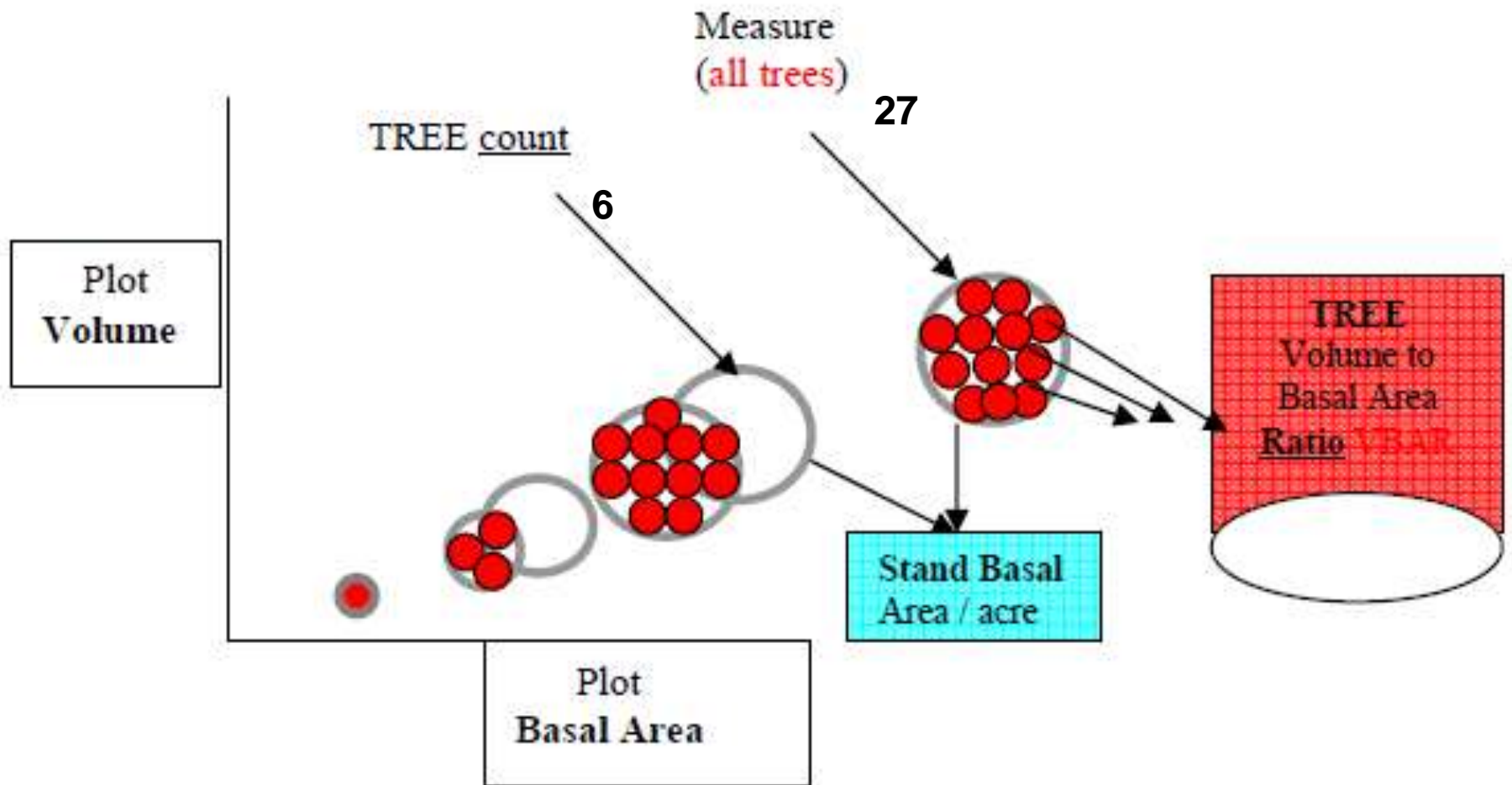
(1) Find BA *somehow* ... ft^2

(2) Find the VBAR *somehow* ... BF/ft^2

(3) **Multiply** them together ... **BF**

This clearly separates steps (1) and (2), *although we often do both on the same sample points.*

The “Product Estimator”



Easy Statistics : (Bruce's Formula)

$$\text{SE\% combined} = \sqrt{(\text{SE\% basal area plots})^2 + (\text{SE\% VBAR trees})^2}$$

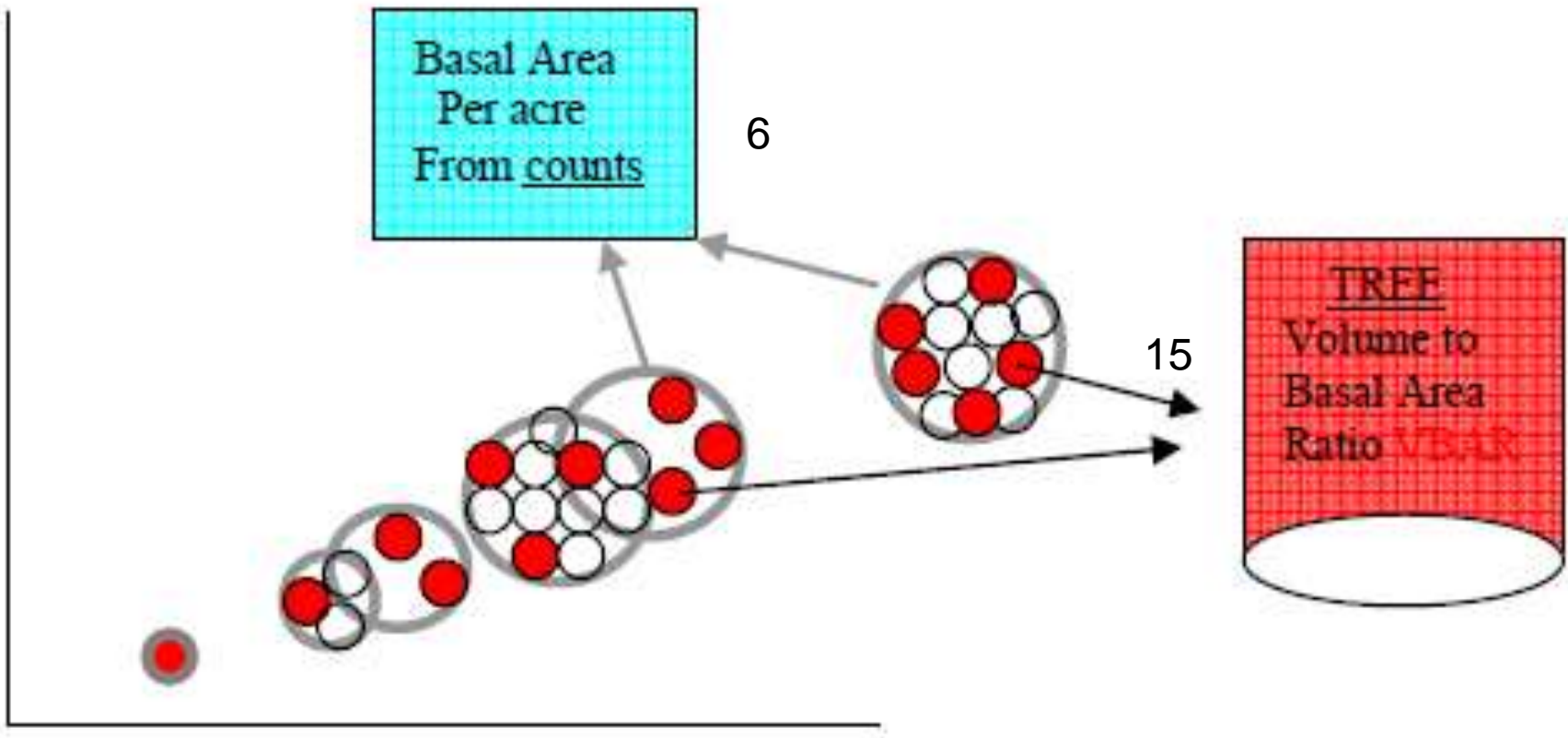


A 30 year gap ...

Finally - Big BAF sampling (1980)

- Now you systematically “spread out” the trees through the stand, and get about double the affect of taking trees in clumps on “measure plots”.
- The advantage is the **Systematic Sampling**

BIG BAF : Spread out the tree measurements



At every plot

- Choose the trees to count by a small angle, this gives you the stand basal area.
- Choose just a few measured trees with a large angle to find out their Volume/BA ratio.
- If the BAF is 5 times larger, you get 1/5th the trees, and they are closer and easy to see.
- Other methods to “spread out” VBARs
(see the John Bell Newsletter for these)

How many of each type? (TC vs. VBARs)

- Effort in each type is pretty much given by :

CV of Tree Count vs. CV of VBARs

- **40%** and **30%** indicate [40 counts & 30 trees],
in multiples sufficient for the SE% you want.
- There is a simple EXCEL spreadsheet for the
exact sample size computation.

What data matters?

- It's easy to tell – just add or subtract data and **recompile** the results to see if anything changes.

Beliefs do not matter here ...

this is algebra, not theology

It is usually the case that you need more counts.

What will more measured trees do for you?

- Tree measurements will give better percentages of log products.
- Products will never be known better than the basal area they are multiplied by.
- All totals will change proportionally with BA for virtually all variables (BF, Grade, \$, etc).

What will more Count Plots do for you?

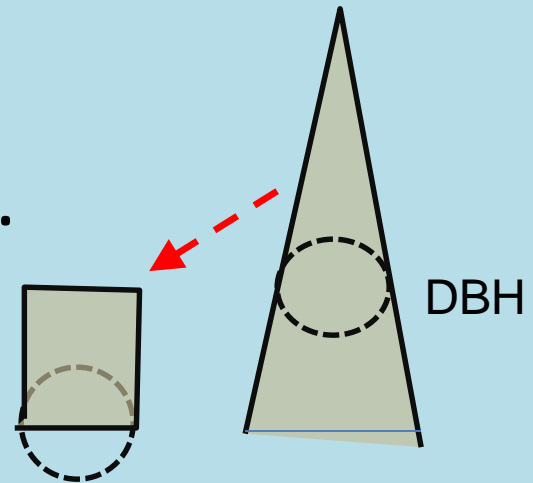
- Tree measurements will give better percentages by species and better BA.
- Much better efficiency for the cruise.
- Better totals of anything that uses Basal Area in its compilation (almost everything).

VBAR

- Usually done by measuring a tree for its total volume, then dividing by that tree's basal area at DBH.

$$\text{VBAR} = \text{Volume} / \text{tree basal area} = \text{BF}/\text{ft}^2.$$

- “Solid cylinder height”
- There are other ways as well.



Another way to get VBAR

- Estimate the logs in the tree (MB&G, 1950's) for logs/ft², then measure BF/log to correct that.

The extra units cancel out ...

$$\cancel{\text{ft}^2}/\text{acre} * \cancel{\text{logs}/\text{ft}^2} * \text{BF}/\cancel{\text{log}} = \text{BF}/\text{acre}$$

More ways to get **VBAR**

- Use a **percentage of tree or stand height**
roughly (**2 * total tree height**) = BF/ft²
For cubic (**Ht/3**) = ft³/ft²
- Use the vertical distance to where the tree is
“borderline” (“**critical height**” ... Relascope).
- Use “**Pressler’s Height**” (use Relascope).
- Use **historical data** .

What data should you see?

- Any computer program needs to report how variable the **TC** and **VBAR** are.
(The “CV” statistic for each).
VBAR can be any tree measurement divided by the tree basal area (giving statistics).
- The program should give you the measured tree data, so you can research it on your own.

What is next?

- **3P sampling, which :**

Makes quick estimates for everything.
then corrects those estimates.

3P is good for anything, not just trees.

Thanks for your patience

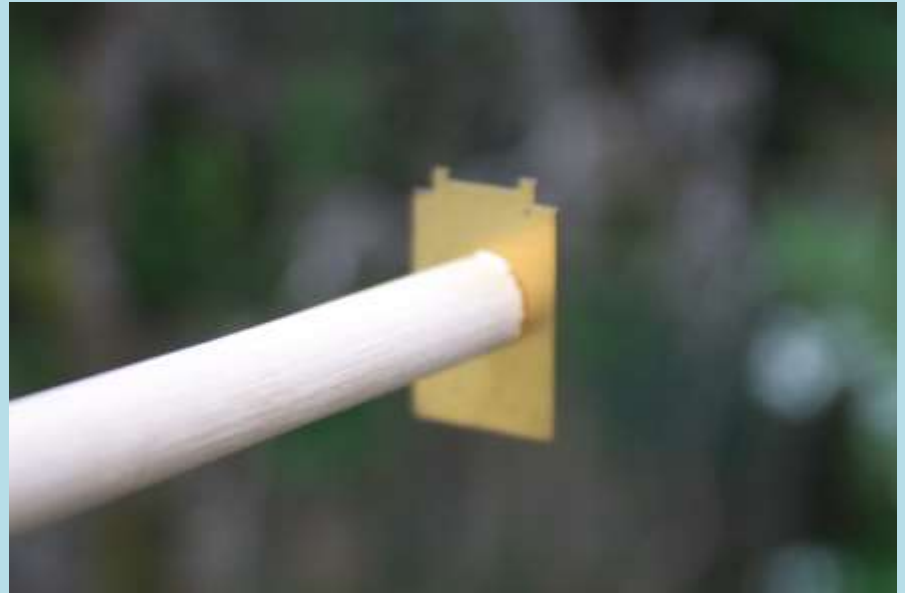
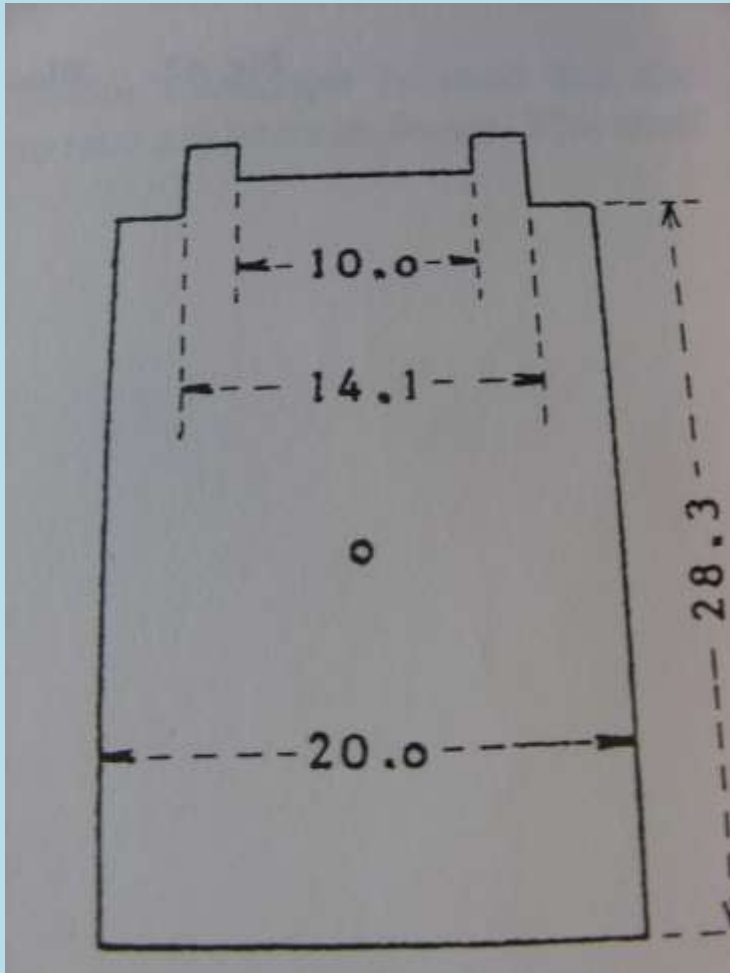
I know it's not scaling, but

You are the timber measurements society.

**Some instruments of cruising,
for you to look over later.**



The first Relascope target



Bitterlich wanted this target etched on his tombstone



Bitterlich's first Relascope



Bitterlich's Wooden Relascope



The 8-power Relascope



The Bitterlich teaching tool

2, 3, and 4 dimensional VP sampling



The first “wedge prism”



The first published prism (6X)



Also, some handouts on ...

- **VP sampling** (and the story of its development, according to Bitterlich)
- **Prism Cruising**
- Story of the development of it (by Bruce)

